

# 2.3.1

## **ALGORITHMS FOR THE MAIN DATA STRUCTURES TOPIC WISE EXAM QUESTIONS**

**A-LEVEL**

**OCR**

1 A tree is one example of a data structure.

(a) (i) Give **two** characteristics of a tree data structure.

1 .....

.....

2 .....

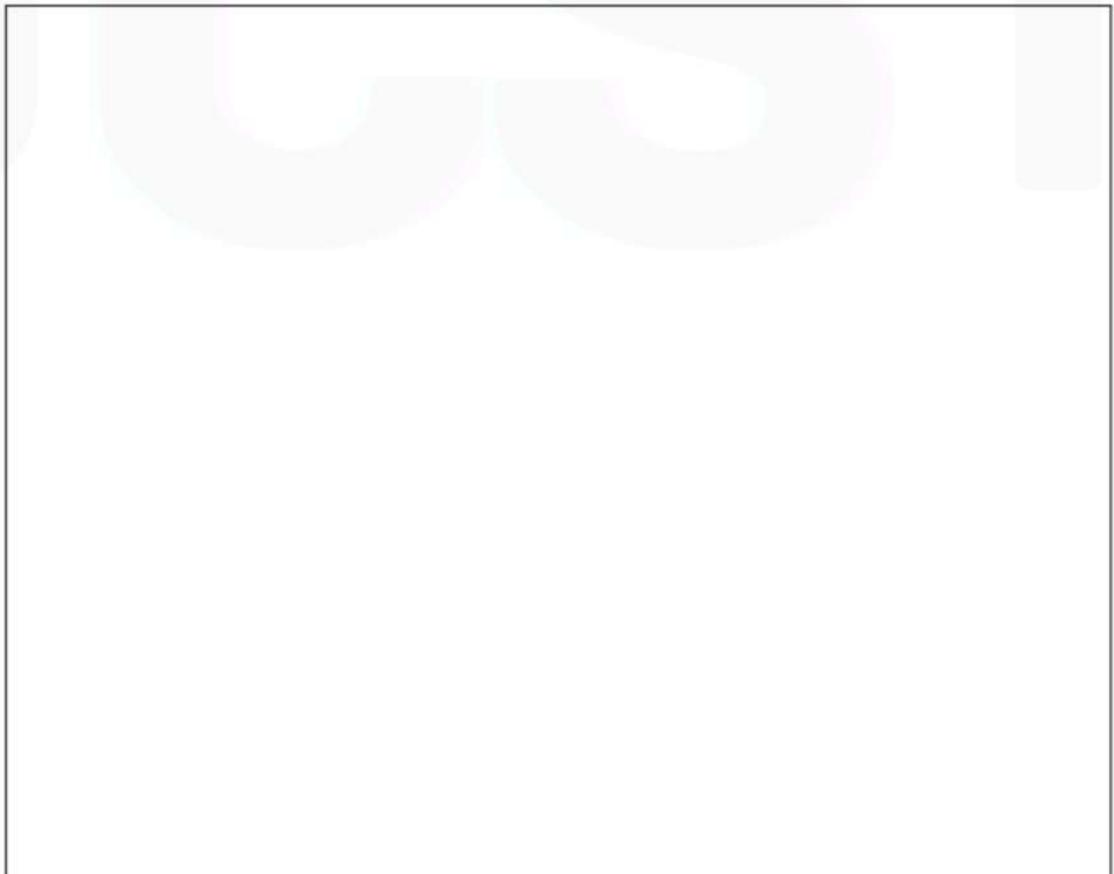
.....

[2]

(ii) The following data is entered into a binary search tree.

22    13    5    36    55    14    8

Draw the binary search tree when the given data is entered in the order given.



[4]

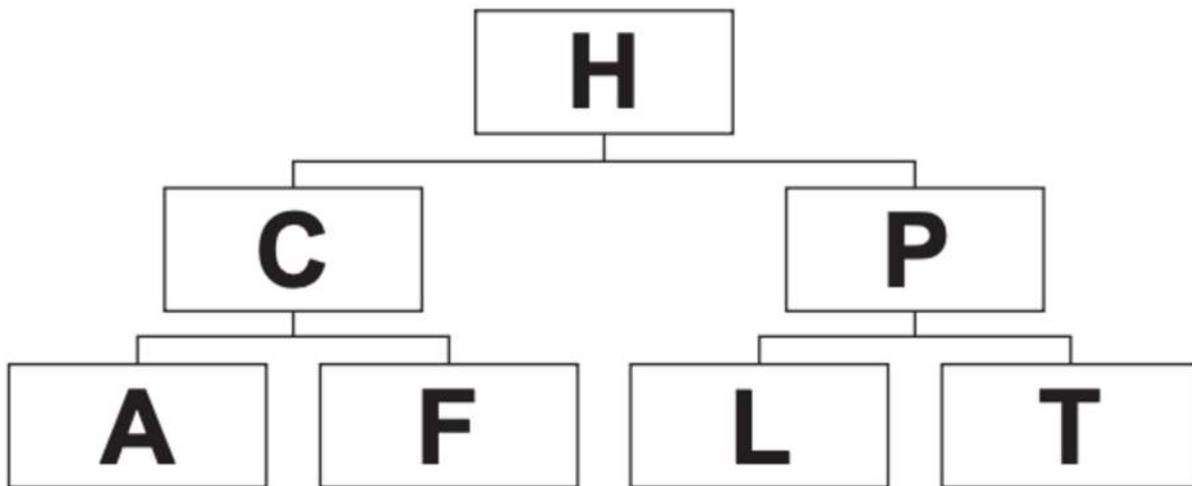
(iii) Describe how a **leaf node** is deleted from a binary search tree.

.....  
.....  
.....  
..... [2]

(iv) Describe how a binary search tree can be searched for a value.

.....  
.....  
.....  
.....  
.....  
.....  
.....  
..... [4]

(v) Identify the order that the nodes will be visited in a **depth-first (post-order)** traversal of this binary search tree.



..... [4]

(vi) Explain how backtracking is used in depth-first (post-order) traversals.

.....  
.....  
.....  
.....  
..... [2]

3 A program stores data in a linked list.

The current contents of the linked list are shown in **Fig. 3**, along with the linked list pointers.

<b>headPointer</b>	1
<b>freeListPointer</b>	4

location	data	pointer
0	"blue"	6
1	"red"	0
2	"green"	8
3	"orange"	NULL
4		5
5		7
6	"grey"	2
7		9
8	"purple"	3
9		NULL

**Fig. 3**

(a) State the purpose of `headPointer` and `freeListPointer` in the linked list shown in **Fig. 3**.

`headPointer` .....

.....

`freeListPointer` .....

.....

[2]

(b) State the meaning of the pointers with the value `NULL` in the linked list shown in **Fig. 3**.

.....

..... [1]

(c) A procedure outputs the data in the linked list shown in **Fig. 3** from the first item in the list, to the last item.

Give the output from the procedure.

.....

..... [2]



2 A computer program is being written to store data about students.

Fig. 2 shows a binary search tree that stores data about students.

Each student is represented by their ID number. The current contents of the binary search tree are:

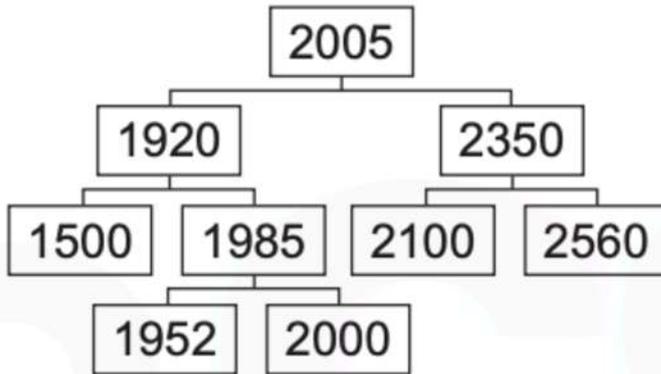


Fig. 2

(a) Identify the root node in the binary tree shown in Fig. 2.

.....  
..... [1]

(b) Identify **two** leaf nodes in the binary tree shown in Fig. 2.

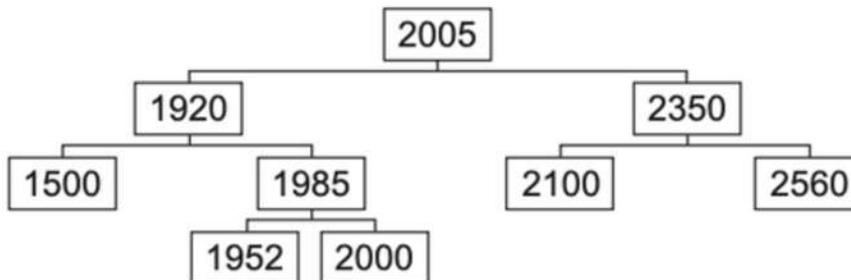
1 .....

2 ..... [2]

(c) Four more students are added to the binary search tree shown in Fig. 2 in this order:

1420 2050 2780 2600

Complete the binary search tree here by adding the new students to it.





- 8 A computer uses a stack data structure, implemented using an array, to store numbers entered by the user.

The array is zero based and has 100 locations.

- (a) Fig. 8 shows the current contents of the stack and the first 9 locations of the array.

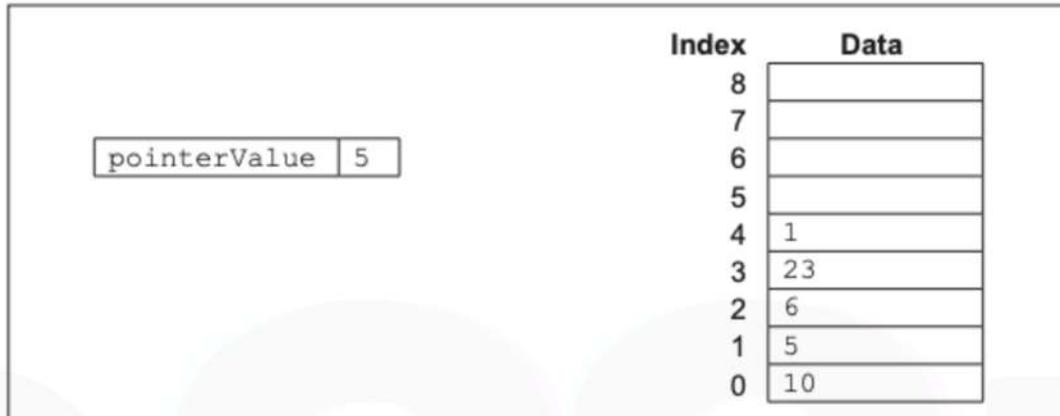


Fig. 8

- (i) The function `pop()` removes an item from the stack.

The function `push()` adds an item to the stack that is passed in as a parameter.

Show the contents of the stack and pointer from Fig. 8 after the following subroutines calls have run.

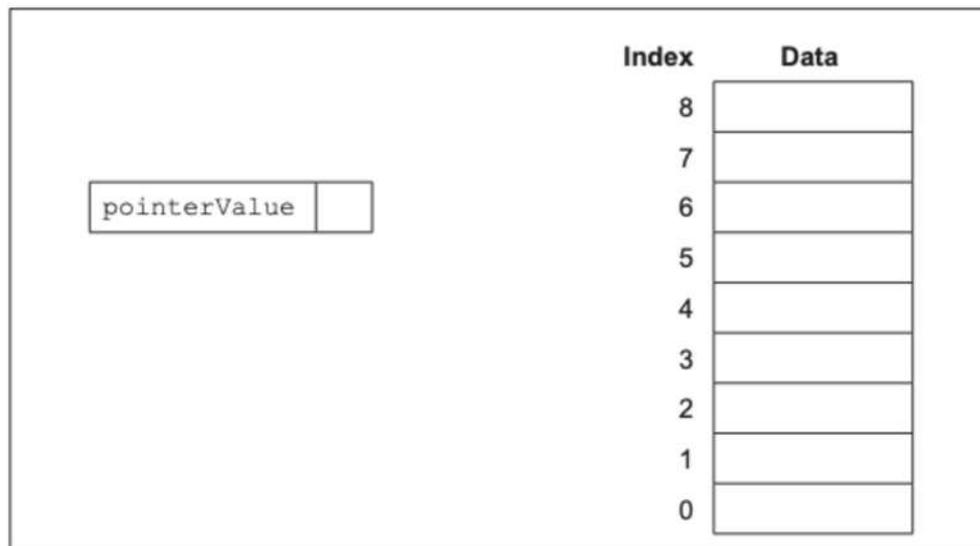
`pop()`

`pop()`

`push(3)`

`push(6)`

`push(7)`



[2]

- (ii) State the purpose of `pointerValue`.





(c) The program is amended to include the use of several queue data structures.

(i) Describe how an array can be used to implement a queue data structure.

.....

.....

.....

.....

.....

..... [3]

(ii)\* Discuss the use of object-oriented programming and procedural programming to create and manipulate the queue data structures.

You should include the following in your answer:

- the features of object-oriented programming
- the features of procedural programming
- the benefits of using object-oriented instead of procedural programming when creating several queue structures. [9]

.....

.....

.....

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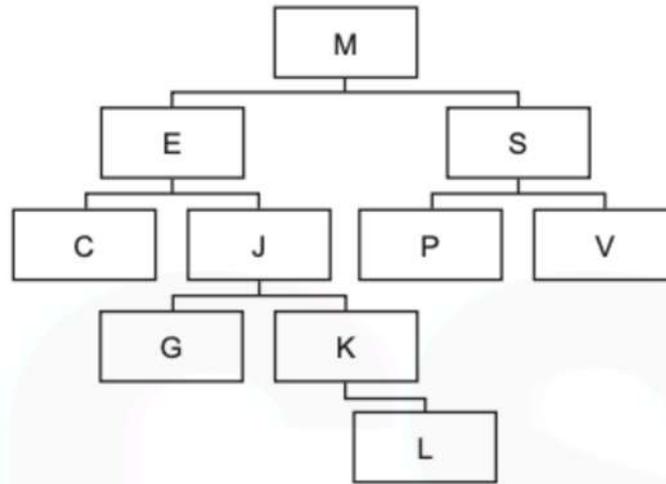
.....

.....

.....

1 (d) A breadth-first traversal can be performed on both a tree and a graph.

Show how a breadth-first traversal is performed on the following binary tree.



.....

.....

.....

.....

.....

.....

[6]

7 Lucas writes a program that makes use of a circular queue. The queue stores the data entered into the program. An array is used to represent the queue.

(a) The program needs two pointers to access and manipulate the data in the queue.

State the purpose of the two pointers and give an appropriate identifier for each.

Pointer 1 purpose .....

.....

Pointer 1 identifier .....

.....

Pointer 2 purpose .....

.....

Pointer 2 identifier .....

.....

[4]

(b) Lucas wants a procedure, `enqueue()`, that will add the parameter it is passed to the queue.

Describe the steps the procedure `enqueue()` will follow when adding new items to the queue.

.....

.....

.....

.....

.....

.....

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.....

.....

[5]

1 Kira is creating a computer game where the user can play against the computer.

In each turn, each character can make one move from a selection of possible moves.

Kira uses a tree data structure shown in Fig. 1 to identify the range of possible moves the computer can make from starting position A. Each connection is a move, with each node representing the result of the move.

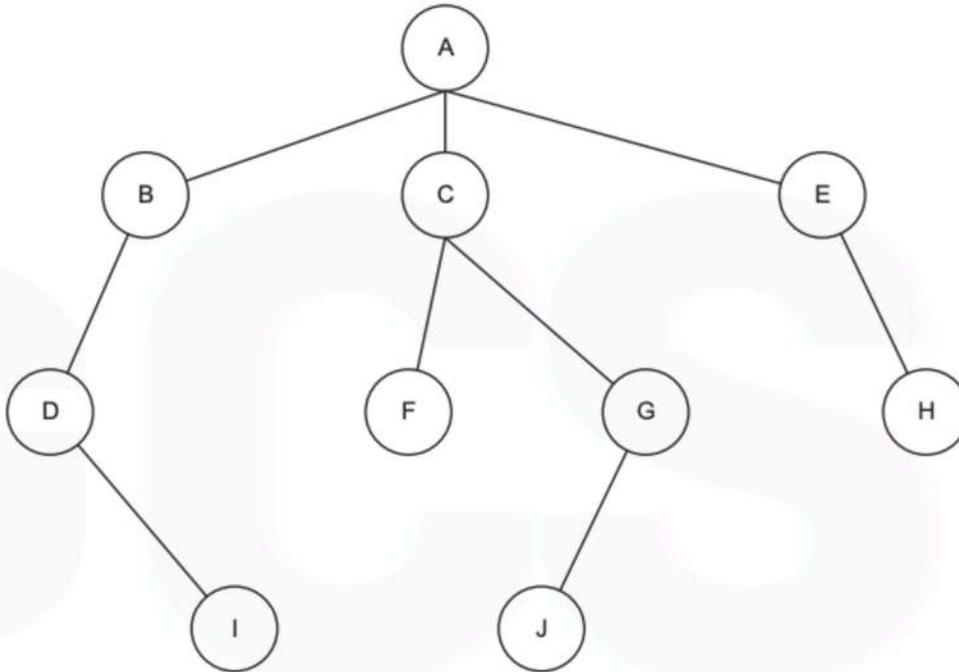


Fig. 1

(b) State why the tree shown in Fig. 1 is **not** an example of a binary search tree.

.....  
..... [1]

(c) State what type of pointers are used to store nodes I, F, J and H so they do not point to any other nodes.

.....  
..... [1]

Kira wants the program to traverse the tree to evaluate the range of possible moves. She is considering using a breadth-first traversal or a depth-first (post-order) traversal.

(d) Show how a breadth-first traversal would traverse the tree shown in Fig. 1.

.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....



- 5 A printer buffer is a storage area that holds the data, known as jobs, that are to be printed by a printer.

A simulation of the printer buffer uses a queue data structure to store jobs that are waiting to be printed. The queue is not circular.

The printer buffer is represented as a zero-indexed 1D array with the identifier `buffer`.

Fig. 2 shows the current contents of the queue `buffer` and its pointers.

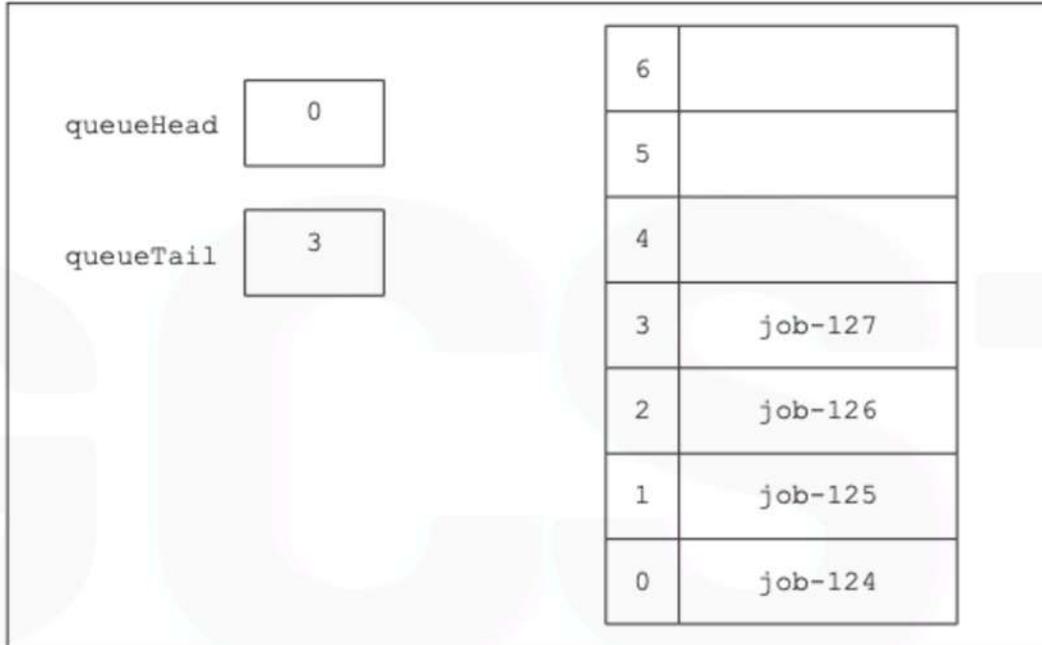


Fig. 2

- (a) State the purpose of the pointers `queueHead` and `queueTail`.

`queueHead` .....

.....

`queueTail` .....

.....

[2]







- 6 Barney is writing a program to store data in a linked list. He is writing the initial program for a maximum of 10 data items.

Each node in the linked list has a data value and a pointer (to the next item).

A null pointer is stored with the value -1.

- (a) Fig. 3 shows the current contents of the linked list including the head and free list pointer values.

	index	data	pointer
headPointer	0	2.6	3
	1	3.5	-1
	2	1.8	1
	3	6.9	2
	4		5
	5		6
	6		7
	7		8
	8		9
	9		-1

freeListPointer 4

Fig. 3

- (i) Describe the purpose of freeListPointer.

.....

.....

.....

..... [2]

- (ii) State the purpose of headPointer.

.....

..... [1]

- (iii) Show the contents of the linked list from Fig. 3 and the pointer values when the node with data 6.9 is deleted.

	index	data	pointer
headPointer			
	0		
	1		
	2		
	3		
	4		
	5		
	6		
	7		
	8		
	9		

freeListPointer



- (d) The procedure `printLinkedList()` follows the pointers to print all of the elements in the linked list.

```
01 procedure printLinkedList(headPointer)
02     tempPointer = headPointer - 1
03     dataToPrint = ""
04     if tempPointer == -1 then
05         print("List is full")
06     else
07         while linkedList[tempPointer].getPointer() != -1
08             dataToPrint = dataToPrint + " " + linkedList[tempPointer,0]
09             linkedList[tempPointer].getPointer() = tempPointer
10         endwhile
11         print(dataToPrint + " " + linkedList[tempPointer].getData())
12     endif
13 endprocedure
```

The procedure has a number of errors.

- (i) Identify the line of each error and write the corrected line.

Error 1 line number .....

Error 1 correction .....

Error 2 line number .....

Error 2 correction .....

Error 3 line number .....

Error 3 correction .....

[3]



3 Oscar owns a taxi company. He would like a program to handle taxi bookings from customers.

(a) When a customer makes a booking, they are placed into a queue data structure until a taxi driver is available.

(i) Explain why Oscar uses a queue data structure rather than a stack data structure.

.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
..... [4]

(ii) Oscar has written a procedure, `enqueue`, to be able to add a customer number to the queue. The queue is not circular.

```
01 procedure enqueue(custNumber)
02   maxElements = 10
03   if (tail + 1) > maxElements then
04     print ("Error, queue is full")
05   else
06     head = head + 1
07     queue[head] = custNumber
08   endif
09 endprocedure
```

State the name of the parameter used in the procedure `enqueue`.

.....  
..... [1]

(iii) The procedure `enqueue` contains an error on line 06 and line 07.

Rewrite lines 06 and 07 of the procedure `enqueue` so that the queue works correctly.

.....  
.....  
.....  
..... [2]

(iv) Identify the logical condition in the procedure `enqueue` that affects whether a new item can be added to the queue.

.....  
..... [1]

- 1 The temperatures of an ocean are input into a computer system. They are recorded, and will be accessed, in the order in which they arrive. The data for one week is shown:

5, 5.5, 5, 6, 7, 6.5, 6

- (a) The data is to be stored in a data structure. The programmer stores the data in a queue.

Explain why a queue is used instead of a stack.

.....  
.....  
.....  
..... [2]

- (b) The data is processed. After processing, the value for the first day is stored as 0. The value for each following day is stored as an increase, or decrease, from the first day.

For example: if the first day was 7, the second was 6 and the third was 9, after processing it would be stored as 0, -1, 2.

- (i) The queue uses `dequeue ()` to return the first element of the queue.

`dequeue ()` is a function.

Explain why `dequeue ()` is a function, not a procedure.

.....  
..... [1]

- (ii) Complete the algorithm to process the data in the queue and store the results in an array called `processedData`.

```
processedData[0] = 0
firstDay = .....
for count = 1 to 6
    processedData[.....] = dequeue () - .....
next count
```

[3]

- 2 A program needs to store the names of plants that are in a garden, so they can be easily found and accessed in alphabetical order.

The data is stored in a tree structure. Part of the tree is shown.

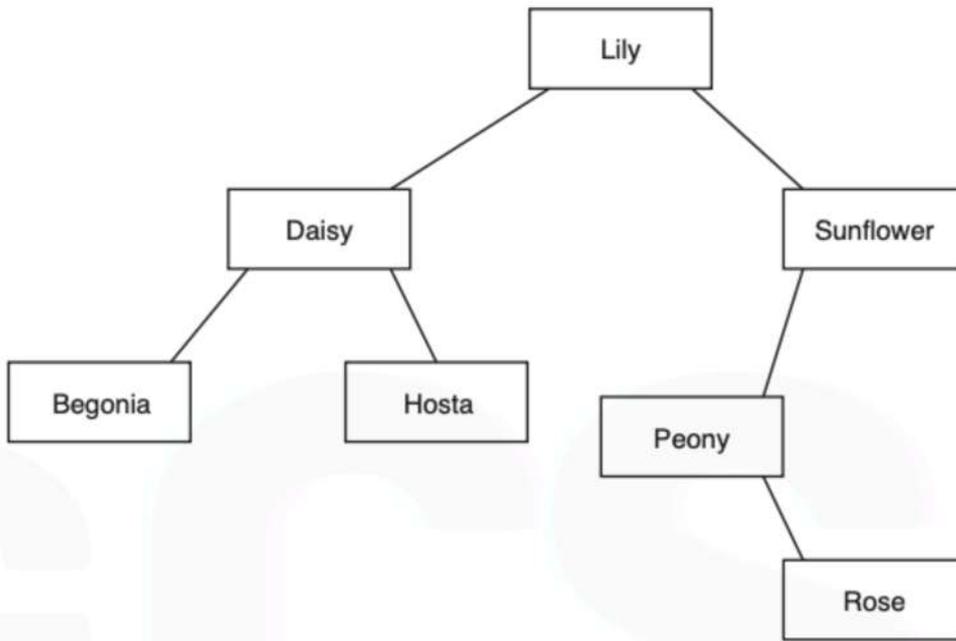


Fig. 2.1

- (a) (i) State the type of tree shown in Fig. 2.1.

..... [1]

- (ii) Show the output of a breadth-first traversal of the tree shown in Fig. 2.1.

.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
..... [3]







3 The current contents of a queue, `colours`, implemented in an array is shown in Fig. 3.1.

red	yellow	green	blue	grey			
-----	--------	-------	------	------	--	--	--

`front = 0`

`end = 4`

Fig. 3.1

(a) Describe the purpose of `front` and `end`.

.....  
.....  
.....  
..... [2]

(b) The queue has the subprograms `enqueue` and `dequeue`. The subprogram `enqueue` is used to add items to the queue and the subprogram `dequeue` removes items from the queue.

(i) Use the following diagram to show the queue shown in Fig. 3.1 after the following program statements have run:

```
enqueue ("orange")  
dequeue ()  
enqueue ("maroon")  
dequeue ()  
dequeue ()
```

--	--	--	--	--	--	--	--

`front = .....`

`end = .....`

[4]

(ii) `enqueue` and `dequeue` are both functions.

State the difference between a procedure and a function.

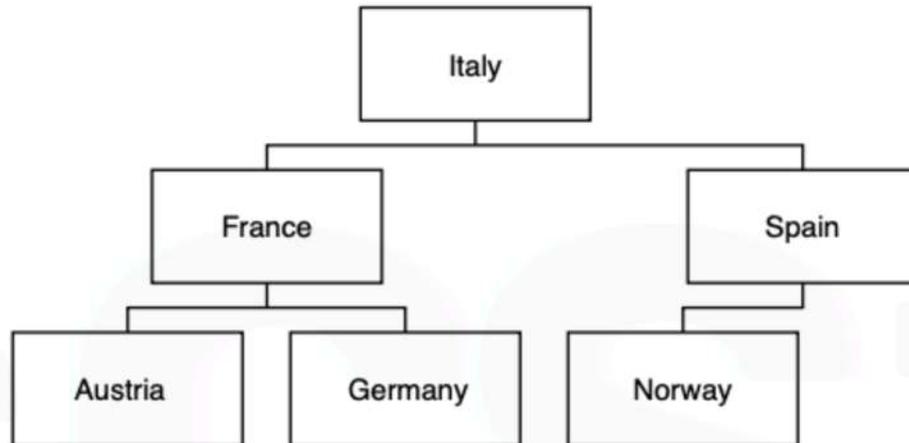
.....  
..... [1]

(iii) Describe the steps involved in the `enqueue` algorithm.

.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
..... [4]

- 1 A program stores entered data in a binary search tree.

The current contents of the tree are shown:



- (a) Complete the diagram to show the contents of the tree after the following data is added:

England, Scotland, Wales, Australia

[3]



- (c) A pseudocode algorithm is written to search the tree to determine if the data item "Sweden" is in the tree.

The function `currentNode.left()` returns the node positioned to the left of `currentNode`.

The function `currentNode.right()` returns the node positioned to the right of `currentNode`.

```
function searchForData(currentNode:byVal, searchValue:byVal)
    thisNode = getData(.....)
    if thisNode == ..... then
        return .....
    elseif thisNode < searchValue then
        if currentNode.left() != null then
            return (searchForData(currentNode.left(), searchValue))
        else
            return .....
        endif
    else
        if ..... != null then
            return (searchForData(currentNode.right(), searchValue))
        else
            return false
        endif
    endif
endfunction
```

- (i) Complete the algorithm.

[5]

- (ii) The algorithm needs to be used in different scenarios, with a range of different trees.

Identify **two** preconditions needed of a tree for this algorithm to work.

1 .....

2 .....

[2]

- 5 A computer program stores data input on a stack named `dataItems`. The stack has two sub-programs to add and remove data items from the stack. The stack is implemented as a 1D array, `dataArray`.

Sub-program	Description
<code>push()</code>	The parameter is added to the top of the stack
<code>pop()</code>	The element at the top of the stack is removed

The current contents of `dataItems` are shown:

6
15
100
23

- (a) Show the contents of the stack `dataItems` after each line of the following lines of code are run

```
01 push(13)
02 pop()
03 push(10)
04 push(20)
```

Line 01	Line 02	Line 03	Line 04
6			
15			
100			
23			

[4]

- (b) The main program asks a user to push or pop an item from the stack. If the user chooses 'push', the data item is added to the stack. If the user chooses "pop", the next item is removed from the stack, multiplied by 3 and output.

The main program is shown:

```
01 userAnswer = input("Would you like to push or pop an item?")
02 if userAnswer == "push" then
03     push(input("Enter data item"))
04 else
05     print(pop() * 3)
06 endif
```

- (i) Before the sub-programs, `push()` and `pop()`, can add or remove items from the stack, a selection statement is used to decide if each action is possible.

Describe the decision that needs to be made in each sub-program and how this impacts the next process.

`push()` .....

.....

.....

.....

`pop()` .....

.....

.....

.....

[4]

- (ii) The algorithm does not work when the user enters "PUSH" or "Push". The algorithm needs to be changed in order to accept these inputs.

Identify the line number to be changed and state the change that should be made.

Line number .....

Change.....

.....

[2]

- (c) The stack is implemented as a 1D array, `dataArray`.

Describe how a 1D array can be set up and used to push and pop items as a stack.

.....

.....

.....

.....

.....

.....

.....

[3]



(ii) Kamran chooses to use a record structure to store the data about the items.

Record structures may be declared using the following syntax:

```
recordStructure recordstructurename  
    fieldname : datatype  
    ...  
endRecordStructure
```

Complete the pseudocode to declare a record called *items*.

```
recordStructure .....  
    itemName : .....  
    .....: Currency  
    .....: Date  
    transferred : .....  
endRecordStructure
```

[5]

(iii) New records may be created using the following syntax:

```
recordidentifier : recordstructurename  
recordidentifier.fieldname = data  
...
```

Write a programming statement to create a new item, using the identifier 'box1', with the item name "Box", the cost 22.58, date of arrival 1/5/2018 and transferred true.

.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....  
..... [3]

- (b) The array, `theItems`, stores the items in the queue. When the tail of the queue exceeds the last element in the array, it adds a new item to the first element if it is vacant.

For example, in the following queue, the next item to be added would be placed at index 0.

Index	0	1	2	3	4	5	6	7	8	9
Element				Data						

- (i) Define the term 'queue'.

.....  
.....  
.....  
..... [2]

- (ii) The attributes in `itemQueue` are all declared as private.

Explain how a private attribute improves the integrity of the data.

.....  
.....  
.....  
..... [2]

- (iii) The constructor method creates a new instance of `itemQueue` and sets the `head`, `tail` and `numItems` attributes to 0.

Write an algorithm, using pseudocode or program code, for the constructor including the initialisation for all attributes.

.....  
.....  
.....  
.....  
.....  
..... [2]





- 1 A user enters whole numbers into a computer program. Each number entered is placed onto a stack. The stack is created using an array with a maximum of 20 elements.

Part of the array, `numStack`, is shown when one number has been input.

top	1
-----	---

index	stackItem
9	
8	
7	
6	
5	
4	
3	
2	
1	
0	20

The pointer, `top`, points to the next free space in the stack.

- (a) Complete the diagram below to show the state of `numStack` after the user inputs the following numbers in the order given:

22    13    2    59    1000

top	
-----	--

index	stackItem
9	
8	
7	
6	
5	
4	
3	
2	
1	
0	20

[2]

(b) A function, `addItem`, takes a number as a parameter and adds the number to the stack. The function returns `true` if this was successful, and `false` if the stack is already full.

(i) Give **one** reason why a function is used instead of a procedure in this scenario.

.....  
..... [1]

(ii) The parameter can be passed by value or by reference.

Describe what is meant by passing a parameter by value and by reference.

By value .....

.....

.....

.....

By reference .....

.....

.....

.....

[4]

(iii) The function `addItem` is written but is incomplete.

Complete the function, `addItem`.

```
function addItem (number)
    if top == ..... then
        return false
    else
        numStack[.....] = .....
        top = ..... + 1
        .....
    endif
endfunction
```

[5]



- 2 A games company has developed a game called Kidz Arrowz. The players throw an arrow at a target board and are awarded different points depending on which circle the arrow lands. Fig. 1 shows the board.

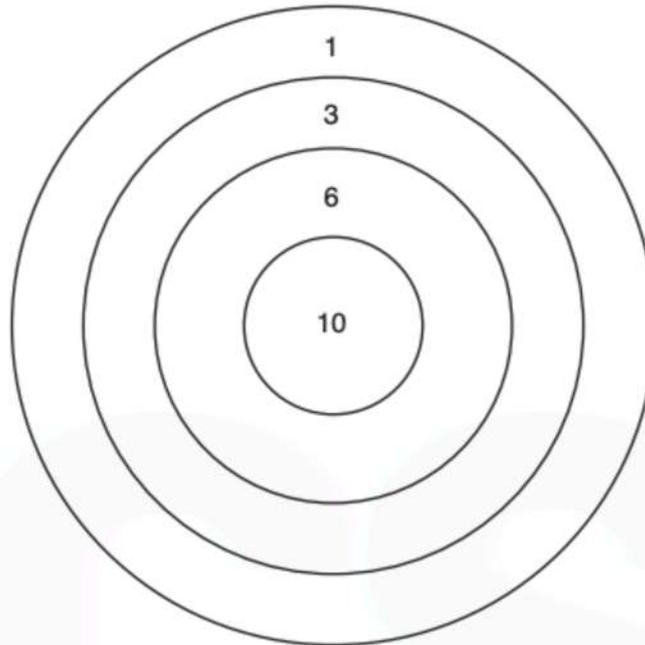


Fig. 1

A computer program is required to keep track of the scores for each competition. The user will enter the number of players, and the name of each player, in that competition to a maximum of 10. The program will then ask for the score of each player in turn. Each competition has 8 rounds, with each player throwing one arrow each round. The program will then display the total score of each player.

- (a) (i) The players are declared as a record structure:

```
record player(string playerName, integer totalScore)
```

Describe what is meant by a record structure.

.....

.....

.....

..... [2]

- (ii) The records for the players are stored in a 1D array.

State why a 1D array is a suitable data structure for the records.

.....

..... [1]

- (iii) Three data structures are arrays, records and stacks.

Identify **one** other data structure.

..... [1]



2 A programmer is developing an ordering system for a fast food restaurant. When a member of staff inputs an order, it is added to a linked list for completion by the chefs.

(a) Explain why a linked list is being used for the ordering system.

.....  
.....  
.....  
..... [2]

(b) Each element in a linked list has:

- a pointer, `nodeNo`, which gives the number of that node
- the order number, `orderNo`
- a pointer, `next`, that points to the next node in the list

Fig. 2.1 shows the current contents of the linked list, `orders`.

nodeNo	orderNo	next
0	154	1
1	157	2
2	155	3
3	156	∅

Fig. 2.1

∅ represents a null pointer.

(i) Order 158 has been made, and needs adding to the end of the linked list.

Add the order, 158, to the linked list as shown in Fig. 2.1. Show the contents of the linked list in the following table.

nodeNo	orderNo	next

[2]

- (ii) Order 159 has been made. This order has a high priority and needs to be the second order in the linked list.  
Add the order, 159, to the original linked list as shown in Fig. 2.1. Show the contents of the linked list in the following table.

nodeNo	orderNo	next

[3]

- (c) The linked list is implemented using a 2D array, `theOrders`:

- Row 0 stores `orderNo`
- Row 1 stores `next`

The data now stored in `theOrders` is shown in Fig. 2.2.

184	186	185	187
1	2	3	

Fig. 2.2

`theOrders[1,0]` would return 1

The following algorithm is written:

```

procedure x()
    finished = false
    count = 0
    while NOT(finished)
        if theOrders[1,count] == null then
            finished = true
        else
            output = theOrders[0,count]
            print(output)
            count = theOrders[1,count]
        endif
    endwhile
    output = theOrders[0,count]
    print(output)
endprocedure

```

(i) Outline why `nodeNo` does not need to be stored in the array.

.....  
..... [1]

(iv) A new order, 190, is to be added to `theOrders`. It needs to be the third element in the list.

The current contents of the array are repeated here for reference:

184	186	185	187		
1	2	3			

Describe how the new order, 190, can be added to the array, so the linked list is read in the correct order, without rearranging the array elements.

.....  
.....  
.....  
.....  
.....  
.....  
.....  
..... [4]

- 3 An encryption routine reads a line of text from a file, reverses the order of the characters in the string and subtracts 10 from the ASCII value of each letter, then saves the new string into the same file.

The program is split into sub-procedures. Three sub-procedures are described as follows:

- Read string from file
- Push each character of the string onto a stack
- Read and encrypt each character message

- (c) A function, `push`, can be used to add a character to a stack. For example:

```
theStack.push("H")
```

places the character `H` onto the stack, `theStack`.

A procedure, `pushToStack`, takes a string as a parameter and pushes each character of the message onto the stack, `messageStack`.

Complete the procedure below.

Add comments to explain how your code works.

```
procedure pushToStack(message)
```

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

```
endprocedure
```

[5]

- (d) Describe the steps that the program would have to take in order to encrypt the characters stored in the stack, and save them in a single variable.

.....

.....

.....

.....

.....

.....

.....

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.....

.....

.....

[5]

4 A data structure is shown below in Fig. 4.1.

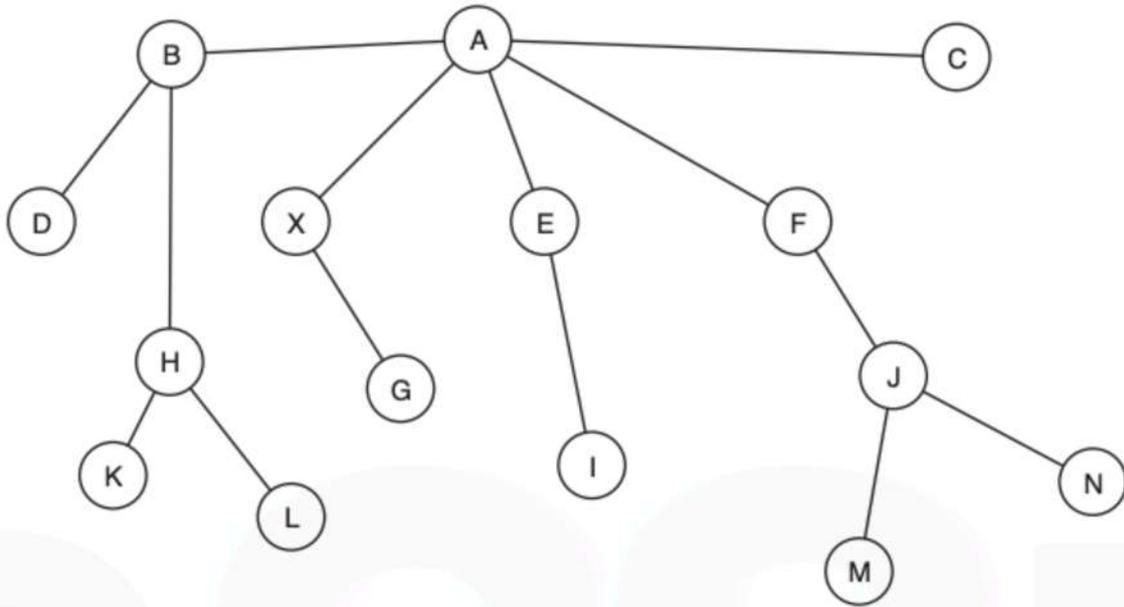


Fig. 4.1

(a) Identify the data structure shown in Fig. 4.1.

..... [1]

(b) The programmer is considering using a depth-first (post-order) traversal, or a breadth-first traversal to find the path between node A and node X.

(i) Explain the difference between a depth-first (post-order) and breadth-first traversal.

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.....  
..... [4]





(c) Complete the following algorithm, to remove, and output, the first element in the queue.

```
procedure remove()
```

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.....

.....

```
endprocedure
```

[4]

(d) Complete the following algorithm, to ask the user to input a new question and then either add it to the queue, or report that the queue is full.

```
procedure add()  
    maxElements = 10
```

.....

.....

.....

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.....

.....

.....

```
endprocedure
```

[4]



**If you found this  
useful, drop a follow  
to help me out!**

**THANK YOU!**

**GCST**